

# Combined analysis of free and forced nutations from VLBI group delays

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# Nutation estimation from VLBI

- VLBI measures antenna voltage and time
- Voltage data are correlated and Fourier transformed
- Correlation function spectrum is used to compute group delays
- **Group delays are used for estimation of daily nutation offset time series**
- **Nutation time series is used for deriving nutation spectrum**
- **Nutation spectrum is used for evaluation of BEPs**

Do we need last three separate steps?

# Deficiencies of the traditional approach

- Correlations between parameters are neglected  
Consequences:
  - Estimates are not optimal
  - Uncertainties are biased
- Change in nutation during experiment is neglected
- Forced nutations and free nutation are treated differently and inconsistently.

# Alternative: direct approach

- . . .
- **Group delays are used for estimation of BEPs**

. . .

**Group delays are used for estimation of Earth rotation spectrum**

. . .

**Group delays are used for estimation of the resonant curve**

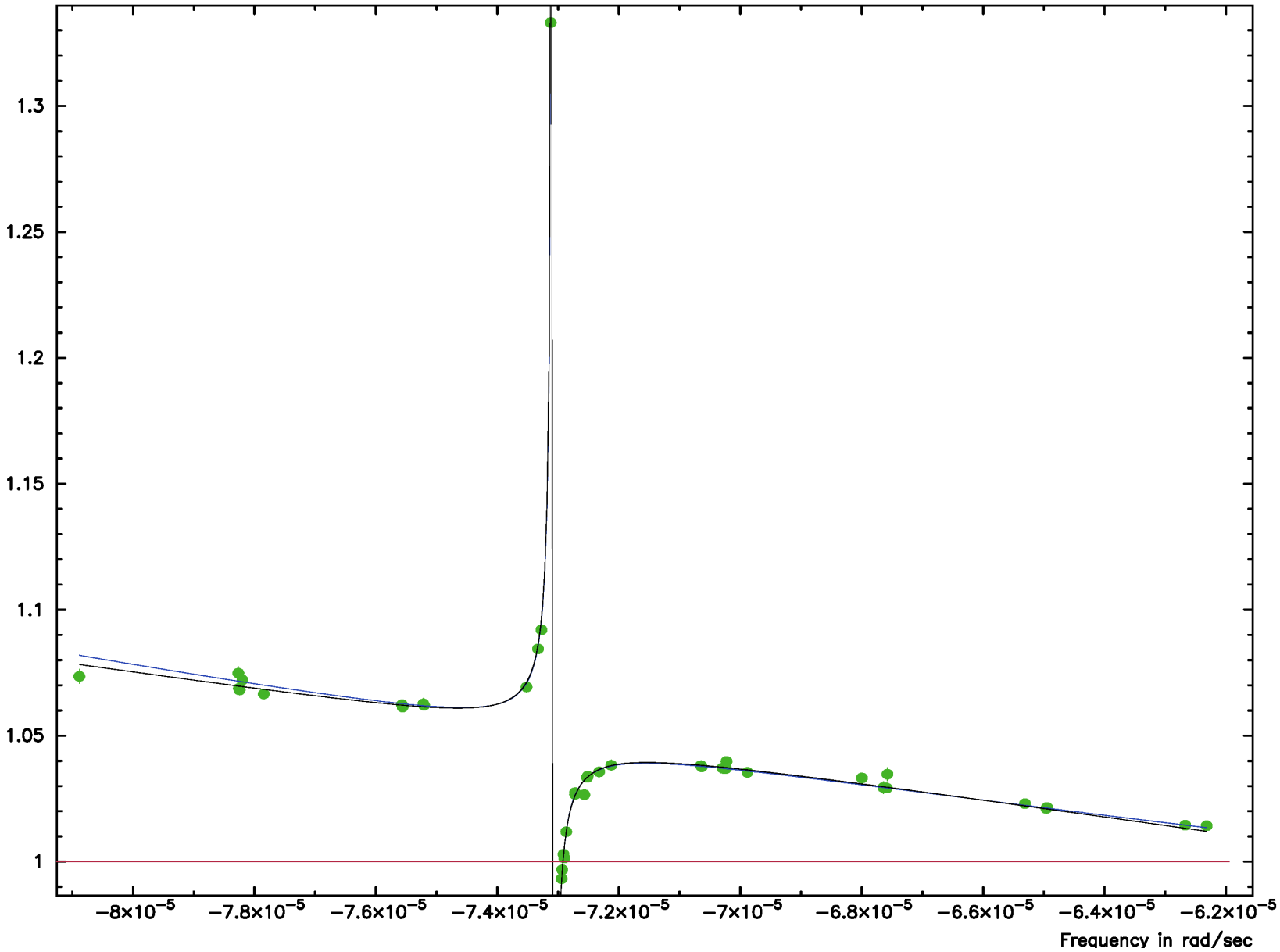
# Spectrum estimation: details

- Estimation of complex spectrum for polar motion ( $E_1 + i E_2$ ), and real valued axial rotation ( $E_3$ )
- Crafting the sequence of frequencies:
  - major forced nutations
  - tidal frequencies
  - dense sampling ( $f = f_0 + i 1/T$ ) within the FCN and PIFCN bands
  - ad hoc frequencies cusps around major tidal spectral lines, ter-diurnal signal around  $S_3-K_3$ , etc
  - adding constraints to unresolved spectral multiplets
- Estimation of limited EOP spectrum in a global solution. Nutations and high-frequency EOP are captured.

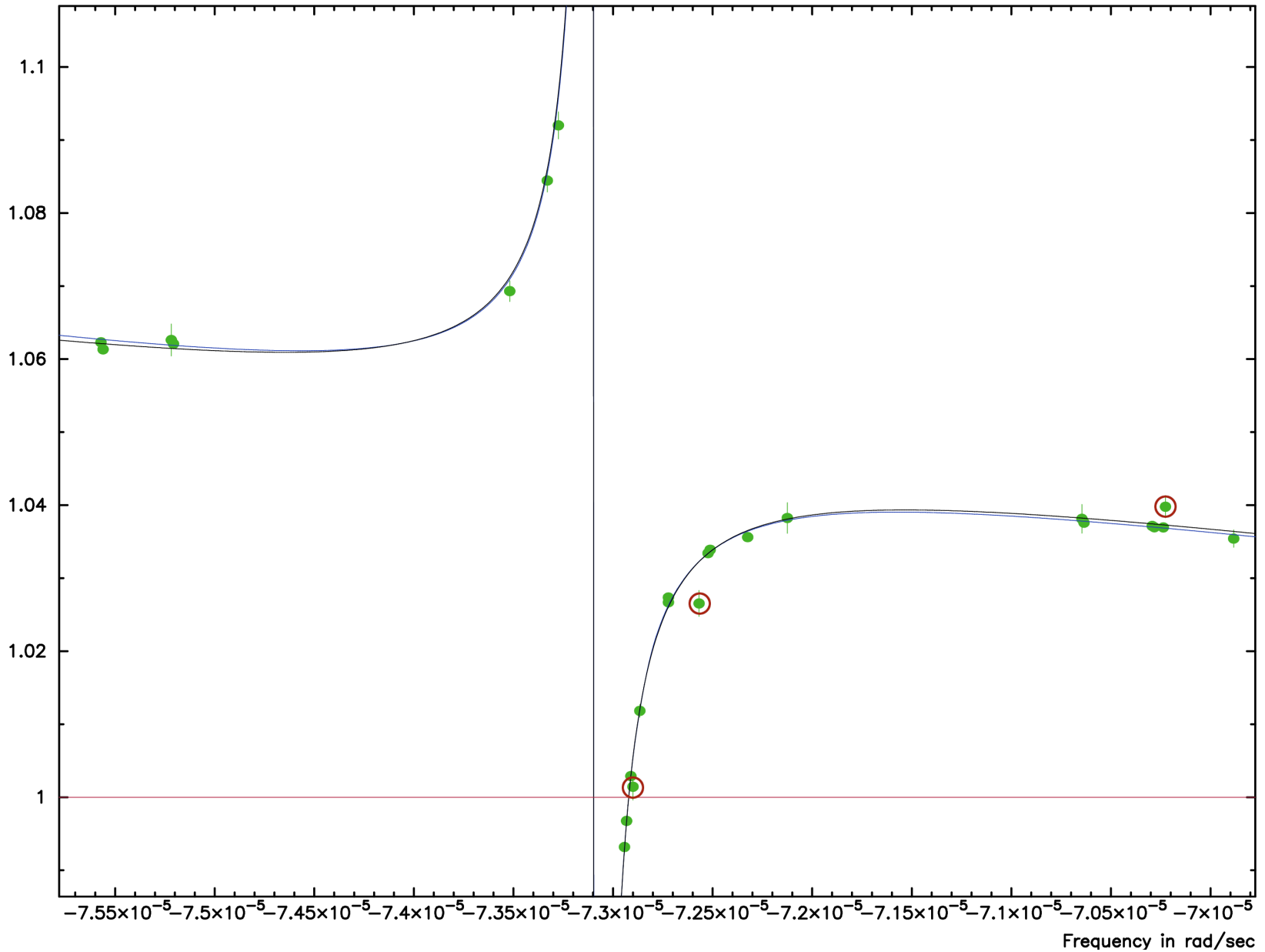
# Spectral analysis

- Fitting the forced nutation spectrum
- Incorporation of OAM and AAM
- Fitting the forced nutation spectrum + the FCN

# Empirical transfer function (Real part)

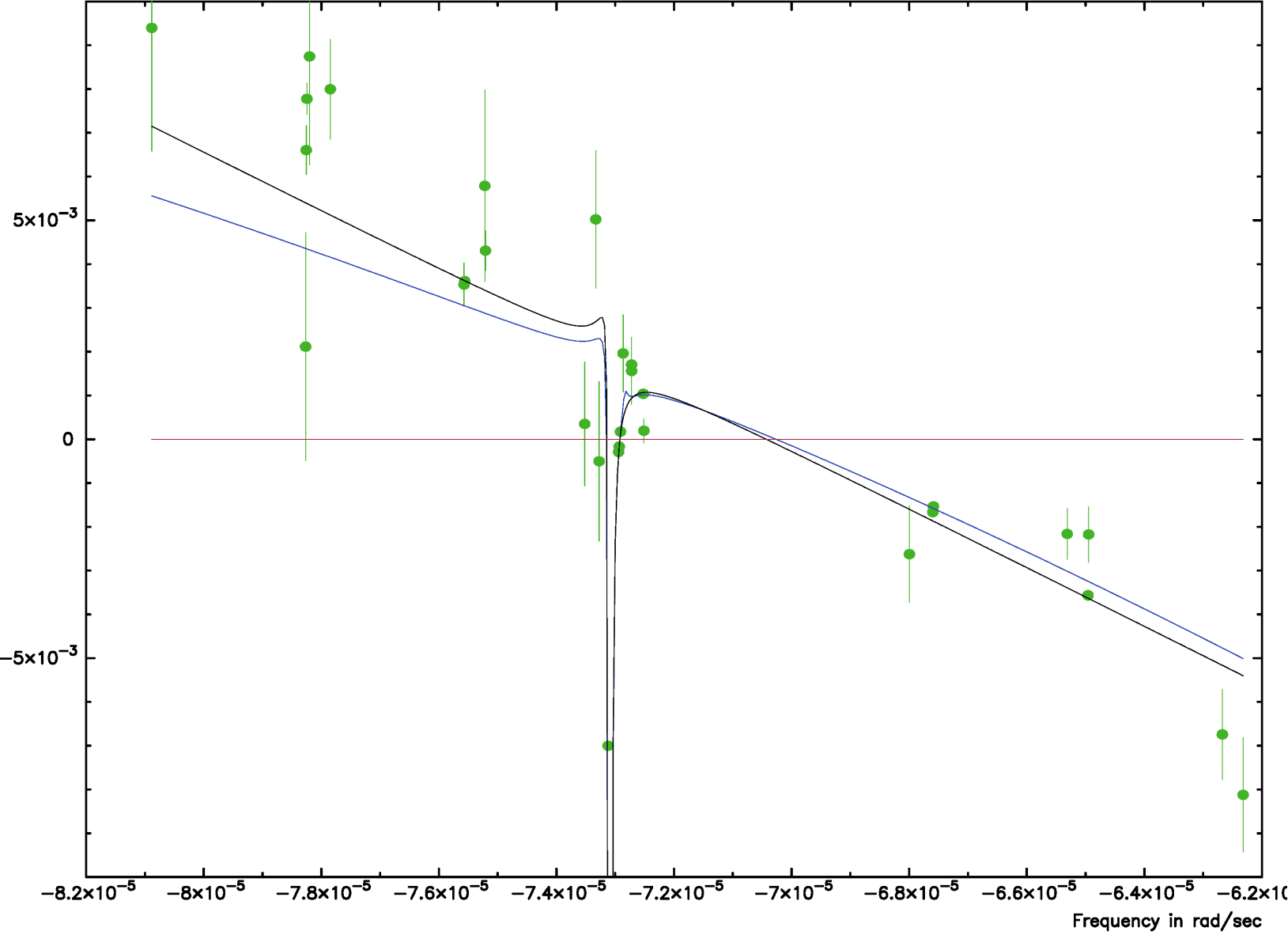


# Empirical transfer function, real part (zoom)

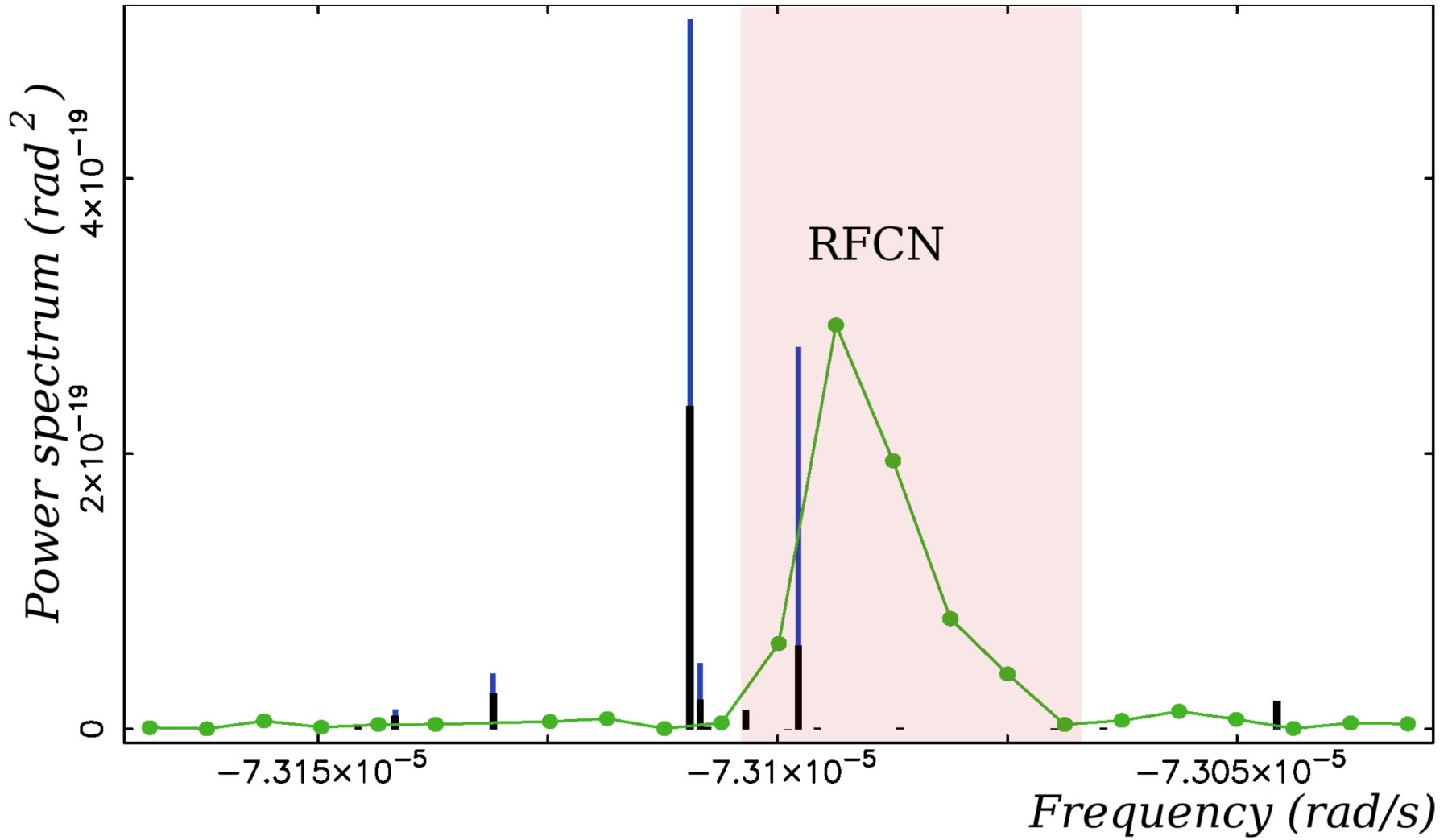




# Empirical transfer function (Imaginary part)



# Free core nutation spectrum



# Putting into play geophysical excitations

AAM:

- Take NASA GEOS-FPIT model ( $0.625^\circ \times 0.5^\circ \times 3^h \times 72$  layers)
- Extrapolate beneath the model surface layer
- Expand into B-spline basis
- Re-grid to the regular  $2' \times 2'$  grid
- Interpolate to the high-resolution surface
- Integrate AAM at the B-spline basis
- Compute the AAM spectrum

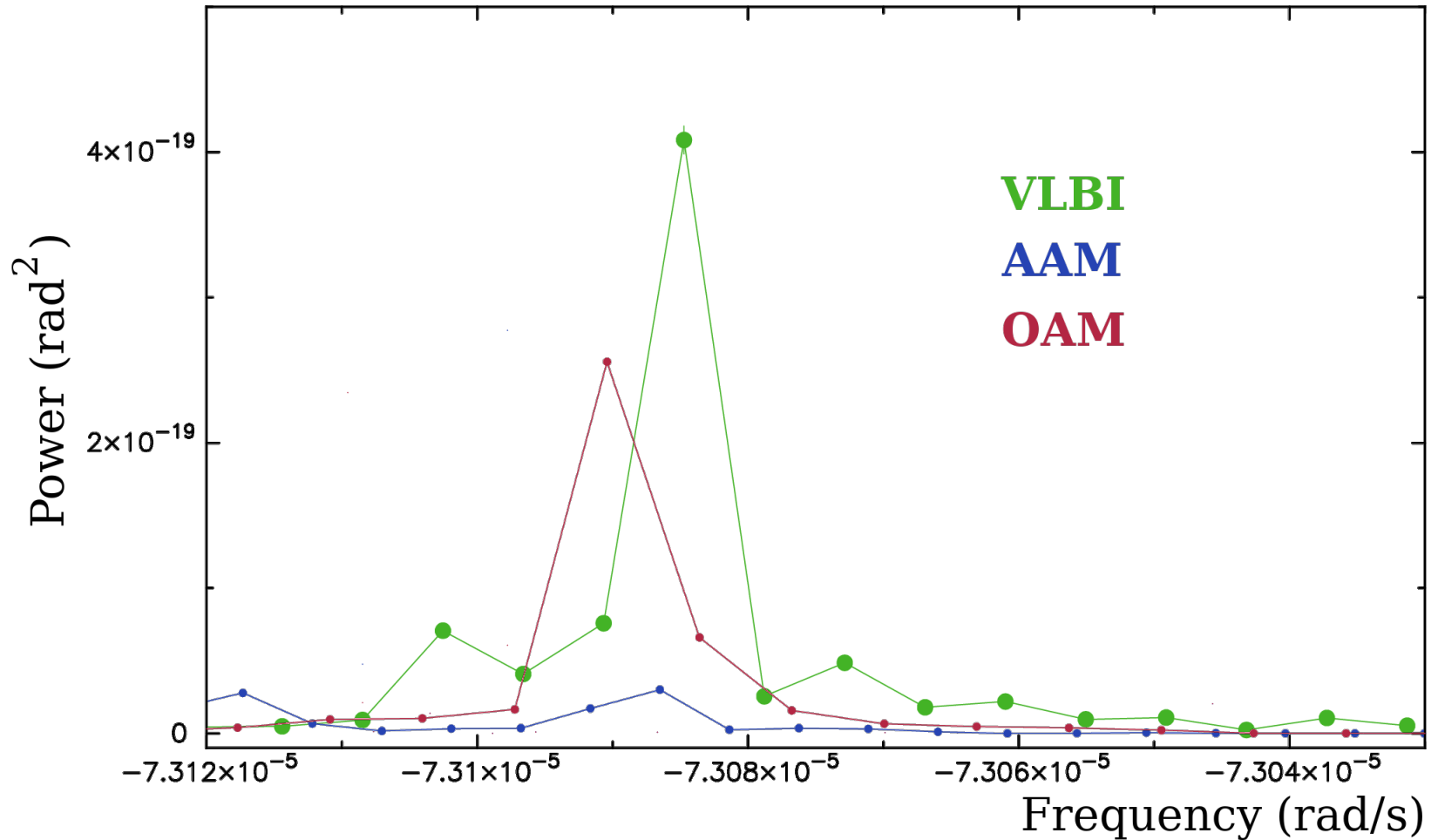
# OAM:

- pressure term
- motion term (current)
- tidal and non-tidal contribution

# EOP, AAM, and OAM spectra

Resonant frequency is derived from forced nutations

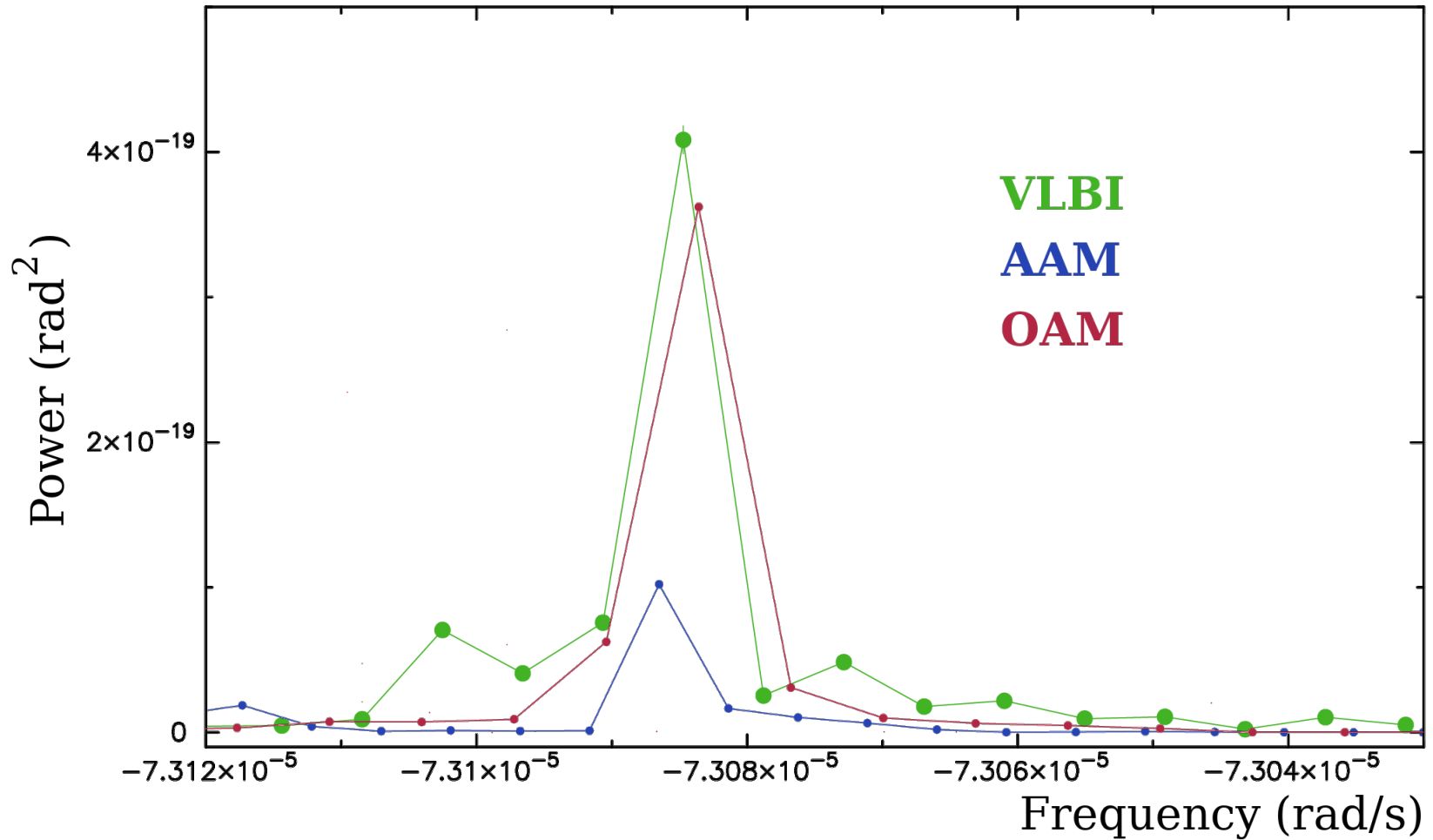
Polar motion spectrum in the FCN band



# EOP, AAM, and OAM spectra

Resonant frequency is derived from the free nutation

Polar motion spectrum in the FCN band



# Summary:

- We can directly estimate of the EOP spectra from group delays
- Effect of the ocean tides still needs improvement
- We may close the FCN excitation budget by accounting for ocean and atmospheric excitation